## The axial-vector meson in coupled-channel approach



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(1) Motivation
(2) Formalism
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## Motivation

- The axial-vector meson
- The existence of $a_{1}$ meson was proven experimentally around four decades ago. [ C.Daum (ACCMOR), PLB89, 281 (1980)]
- Until now the uncertainty of its mass and width are still large.
- Their nature is still unclear. Composite? Elementary?


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- Their nature is still unclear. Composite? Elementary?


$$
\begin{array}{lll}
I=0 & h_{1}(1170) 0^{-} & f_{1}(1285) 0^{+} \\
I=1 & b_{1}(1235) 1^{+} & a_{1}(1260) 1^{-} \\
I=1 / 2 & K_{1}(1270) &
\end{array}
$$

## Motivation

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- Until now the uncertainty of its mass and width are still large.
- Their nature is still unclear. Composite? Elementary?
- The full off-shell $T$ matrix of this interaction can then be applied to other processes as an elementary process.
- $D \bar{D}$ and $D \bar{D}^{*}$ process
- $N \rightarrow \Delta$ axial-vector form factor
- $\Omega$ baryon radiative form factor
- $\tau$ decay
- etc


## Formalism

## Blanckenbecler-Sugar Scheme

We start from the $S$ matrix, $S=1+i T$, which can be written as

$$
S_{f i}=\delta_{f i}-i(2 \pi)^{4} \delta^{4}\left(P_{f}-P_{i}\right) \mathcal{T}_{f i}
$$

The Bethe-Salpeter equation for two-body interaction expressed as

$$
\mathcal{T}_{f i}\left(p^{\prime}, p\right)=\mathcal{V}_{f i}\left(p^{\prime}, p\right)+\frac{1}{(2 \pi)^{4}} \int d^{4} q \mathcal{V}_{f g}\left(p^{\prime}, q\right) \mathcal{G}_{g}(q) \mathcal{T}_{g i}(q, p)
$$



The unitarity requirement of $S$ matrix bring us to Blanckenbecler-Sugar scheme. [ R. Blankenbecler, PR142, 1051 (1966)]

$$
\mathcal{G}_{g}(q)=\delta\left(q_{0}-\frac{E_{1 g}}{2}+\frac{E_{2 g}}{2}\right) \frac{\pi}{E_{1 g} E_{2 g}} \frac{E_{g}}{s-E_{g}^{2}}
$$

## Blanckenbecler-Sugar Scheme

We start from the $S$ matrix, $S=1+i T$, which can be written as

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$$



The unitarity requirement of $S$ matrix bring us to Blanckenbecler-Sugar scheme. [ R. Blankenbecler, PR142, 1051 (1966)]

$$
\mathcal{T}_{f i}\left(\mathbf{p}, \mathbf{p}^{\prime}\right)=\mathcal{V}_{f i}\left(\mathbf{p}, \mathbf{p}^{\prime}\right)+\frac{1}{(2 \pi)^{3}} \int \frac{d^{3} q}{2 E_{1 g} E_{2 g}} \mathcal{V}_{f g}(\mathbf{p}, \mathbf{q}) \frac{E_{g}}{s-E_{g}^{2}} \mathcal{T}_{g i}\left(\mathbf{q}, \mathbf{p}^{\prime}\right)
$$

## Potential

The potential is modeled by one meson exchange diagram


Each diagram gives

$$
\mathcal{V}=I S \times F^{2} \times \Gamma_{1} \times \mathcal{P} \times \Gamma_{2}
$$

## Potential

The potential is modeled by one meson exchange diagram

$$
\mathcal{V}=I S \times F^{2} \times \Gamma_{1} \times \mathcal{P} \times \Gamma_{2}
$$

$$
\mathcal{L}_{P P V}=g_{P P V} \operatorname{Tr}\left(\left[P, \partial_{\mu} P\right]_{-} V^{\mu}\right)
$$

Coupling constants :

$$
\mathcal{L}_{V V V}=-\frac{1}{2} g_{V V V} \operatorname{Tr}\left[\left(\partial_{\mu} V_{\nu}-\partial_{\nu} V_{\mu}\right) V^{\mu} V^{\nu}\right]
$$

$$
\mathcal{L}_{P V V}=\frac{g_{P V V}}{m_{V}} \varepsilon^{\mu \nu \alpha \beta} \operatorname{Tr}\left(\partial_{\mu} V_{\nu} \partial_{\alpha} V_{\beta} P\right)
$$

$$
\begin{aligned}
& g_{P P V}^{2} / 4 \pi=0.71 \\
& g_{P V V}^{2} / 4 \pi=1.88
\end{aligned}
$$

Ref: G.Janssen, PRC49, 2763 (1994)
*Note that we choose $g_{P P V}=g_{V V V}$

$$
P=\left(\begin{array}{ccc}
\frac{1}{\sqrt{2}} \pi^{0}+\frac{1}{\sqrt{6}} \eta & \pi^{+} & K^{+} \\
\pi^{-} & -\frac{1}{\sqrt{2}} \pi^{0}+\frac{1}{\sqrt{6}} \eta & K^{0} \\
K^{-} & \bar{K}^{0} & -\frac{2}{\sqrt{6}} \eta
\end{array}\right)
$$

## Potential

The potential is modeled by one meson exchange diagram

$$
\mathcal{V}=I S \times F^{2} \times \Gamma_{1} \times \mathcal{P} \times \Gamma_{2}
$$

Coupling constants :

$$
\mathcal{L}_{P P V}=g_{P P V} \operatorname{Tr}\left(\left[P, \partial_{\mu} P\right]_{-} V^{\mu}\right)
$$

$$
\mathcal{L}_{V V V}=-\frac{1}{2} g_{V V V} \operatorname{Tr}\left[\left(\partial_{\mu} V_{\nu}-\partial_{\nu} V_{\mu}\right) V^{\mu} V^{\nu}\right]
$$

$$
g_{P P V}{ }^{2} / 4 \pi=0.71
$$

$$
\mathcal{L}_{P V V}=\frac{g_{P V V}}{m_{V}} \varepsilon^{\mu \nu \alpha \beta} \operatorname{Tr}\left(\partial_{\mu} V_{\nu} \partial_{\alpha} V_{\beta} P\right)
$$

$$
g_{P V V}{ }^{2} / 4 \pi=1.88
$$

Ref: G.Janssen, PRC49, 2763 (1994)
*Note that we choose $g_{P P V}=g_{V V V}$

$$
V_{\mu}=\left(\begin{array}{ccc}
\frac{1}{\sqrt{2}} \rho_{\mu}^{0}+\frac{1}{\sqrt{2}} \omega_{\mu} & \rho_{\mu}^{+} & K_{\mu}^{*+} \\
\rho_{\mu}^{-} & -\frac{1}{\sqrt{2}} \rho_{\mu}^{0}+\frac{1}{\sqrt{2}} \omega_{\mu} & K_{\mu}^{* 0} \\
K_{\mu}^{*-} & \bar{K}_{\mu}^{*-} & \phi_{\mu}
\end{array}\right)
$$

## Potential

The potential is modeled by one meson exchange diagram

$$
\mathcal{V}=I S \times F^{2} \times \Gamma_{1} \times \mathcal{P} \times \Gamma_{2}
$$

We use static propagator,

$$
\mathcal{P}=\frac{1}{\left(p^{\prime}-p\right)^{2}-m^{2}} \Longrightarrow \frac{-1}{\left(\vec{p}^{\prime}-\vec{p}\right)^{2}+m^{2}}
$$

And the form factor

$$
F\left(n, \vec{p}, \vec{p}^{\prime}\right)=\left(\frac{n \Lambda^{2}-m^{2}}{n \Lambda^{2}+\vec{p}^{2}+\vec{p}^{2}}\right)^{n}
$$

with

$$
\Lambda=\lambda+m
$$

## One-dimensional integral

Through the partial wave decomposition, the BS equation becomes

$$
\mathcal{T}_{\lambda^{\prime} \lambda}^{f i}\left(\mathrm{p}, \mathrm{p}^{\prime}\right)=\mathcal{V}_{\lambda^{\prime} \lambda}^{f i}\left(\mathrm{p}, \mathrm{p}^{\prime}\right)+\frac{1}{(2 \pi)^{3}} \sum_{g, \lambda_{g}} \int \frac{\mathrm{q}^{2} d \mathrm{q}}{2 E_{g 1} E_{g 2}} \mathcal{V}_{\lambda^{\prime} \lambda_{g}}^{f g}(\mathrm{p}, \mathrm{q}) \frac{E_{g}}{s-E_{g}^{2}} \mathcal{T}_{\lambda_{g} \lambda}^{g i}\left(\mathrm{q}, \mathrm{p}^{\prime}\right)
$$

where

$$
\mathcal{V}_{\lambda^{\prime} \lambda}^{f i}\left(\mathrm{p}^{\prime}, \mathrm{p}\right)=2 \pi \int \mathrm{~d}(\cos \theta) d_{\lambda^{\prime} \lambda}^{J}(\theta) \mathcal{V}_{\lambda^{\prime} \lambda}^{f i}\left(\mathrm{p}^{\prime}, \mathrm{p}, \theta\right),
$$

Evaluating this integral by using principal value

$$
\begin{aligned}
\mathcal{T}_{\lambda^{\prime} \lambda}^{f i}\left(\mathrm{p}, \mathrm{p}^{\prime}\right)= & \mathcal{V}_{\lambda^{\prime} \lambda}^{f i}\left(\mathrm{p}, \mathrm{p}^{\prime}\right)+\frac{1}{(2 \pi)^{3}} \sum_{g, \lambda_{g}}\left[\int d E_{g} \frac{\mathcal{F}\left(E_{g}\right)-\mathcal{F}(\sqrt{s})}{s-E_{g}^{2}}\right. \\
& \left.-\frac{\mathcal{F}(\sqrt{s})}{2 \sqrt{s}}\left(\ln \left|\frac{\sqrt{s}+E_{g}^{\mathrm{thr}}}{\sqrt{s}-E_{g}^{\mathrm{thr}}}\right|+i \pi\right)\right]
\end{aligned}
$$

with

$$
\mathcal{F}\left(E_{g}\right)=\frac{1}{2} \mathcal{q}_{\lambda^{\prime} \lambda_{g}}^{f g}(\mathrm{p}, \mathrm{q}) \mathcal{T}_{\lambda_{g \lambda}}^{g i}(\mathrm{p}, \mathrm{q}),
$$

We solved this integral by utilizing matrix inversion method.

## Results and Discussion

# $G=-1$ and $I=1$ <br> $a_{1}$ resonance 

## Diagrams and Parameters

Channels involved : $\pi \rho$ and $K \bar{K}^{*}$
Since $K$ and $K^{*}$ have no definite $G$-parity,

$$
\left|K \bar{K}^{*}(-)\right\rangle=\frac{1}{\sqrt{2}}\left(\left|K \bar{K}^{*}\right\rangle-\left|\bar{K} K^{*}\right\rangle\right)
$$

Potential :

$$
V^{f i}=\left(\begin{array}{cc}
V^{\pi \rho \rightarrow \pi \rho} & V^{K} \bar{K}^{*} \rightarrow \pi \rho \\
V^{\pi \rho \rightarrow K \bar{K}^{*}} & V^{K \bar{K}^{*} \rightarrow K \bar{K}^{*}}
\end{array}\right)
$$

## Diagrams and Parameters

Channels involved : $\pi \rho$ and $K \bar{K}^{*}$

|  | meson | channel | IS | $\lambda(\mathrm{MeV})$ | $n$ |
| :--- | :---: | :---: | ---: | ---: | ---: |
| $\pi \rho \rightarrow \pi \rho$ | $\pi$ | $u$ | 4 | 600 | 1 |
| $\pi \rho \rightarrow K \bar{K}^{*}\left(\bar{K} K^{*}\right)$ | $\rho$ | $t$ | -4 | 600 | 1 |
| $K \bar{K}^{*} \rightarrow K \bar{K}^{*}$ | $K$ | $u$ | -4 | 600 | 2 |
|  | $K^{*}$ | $u$ | $-2(2)$ | 1500 | 1 |
| $K \bar{K}^{*} \rightarrow \bar{K} K^{*}$ | $\rho$ | $t$ | $2(-2)$ | 1110 | 1 |
|  | $\omega$ | $t$ | 1 | 1050 | 1 |
|  | $\phi$ | $t$ | -1 | 1050 | 1 |
|  | $\pi$ | $u$ | 1 | 1700 | 1 |
|  | $\eta$ | $u$ | -3 | 1050 | 1 |
|  | $\rho$ | $u$ | -1 | 1050 | 1 |
|  | $\omega$ | $u$ | 1 | 1050 | 2 |
|  | $\phi$ | $u$ | 2 | 1700 | 2 |

*Note that for $\phi$-exchange diagram the coupling $g$ differ by about $14 \%$

## $a_{1}$ resonance

The singularities arises as a result of integral equation in the region below $K \bar{K}^{*}$ threshold.


## $a_{1}$ resonance



We compare the model to experimental data from charge exchange reaction $\pi p \rightarrow 3 \pi n$.


And define:

$$
\sigma \equiv-C \operatorname{Im}\left[T_{\pi \rho}\left(M_{\pi \rho}\right)\right]
$$

Exp.Data : J.A.Dankowych, PRL46 (1981).
Model: G.Janssen, PRC54 (1996)

## $a_{1}$ properties

- The $a_{1}(1260)$ pole position, $\sqrt{s_{R}}=1170.1-i 104.1[\mathrm{MeV}]$
- Residue and coupling strength can be defined as

$$
\lim _{s \rightarrow s_{R}}\left(s-s_{R}\right) T_{a, b}=R_{a, b}, \quad g_{a}=\sqrt{R_{a, a}}
$$

- The elastic residue and coupling strength of $a_{1}(1260)$ resonance for $S$-wave and $D$-wave are

|  | $S$-wave | $D$-wave | Unit |
| :--- | :---: | :---: | :---: |
| $R_{\pi \rho}$ | $26.68-i 6.54$ | $0.31+i 0.02$ | $\mathrm{GeV}^{2}$ |
| $R_{K \bar{K}^{*}}$ | $37.17-i 4.74$ | $0.09+i 0.16$ | $\mathrm{GeV}^{2}$ |
| $g_{\pi \rho}$ | $5.20-i 0.63$ | $0.56+i 0.02$ | GeV |
| $g_{K \bar{K}^{*}}$ | $6.11-i 0.39$ | $0.37+i 0.22$ | GeV |

## $G=-1$ and $I=0$

## $h_{1}$ resonance

## Diagrams and Parameters

Channels involved : $\pi \rho, \eta \omega, K \bar{K}^{*}$ and $\eta \phi$.

$$
\left|K \bar{K}^{*}(-)\right\rangle=\frac{1}{\sqrt{2}}\left(\left|K \bar{K}^{*}\right\rangle-\left|\bar{K} K^{*}\right\rangle\right)
$$

Potential :

$$
V^{f i}=\left(\begin{array}{cccc}
V^{\pi \rho \rightarrow \pi \rho} & V^{\eta \omega \rightarrow \pi \rho} & V^{K \bar{K}^{*} \rightarrow \pi \rho} & V^{\eta \phi \rightarrow \pi \rho}=0 \\
V^{\pi \rho \rightarrow \eta \omega} & V^{\eta \omega \rightarrow \eta \omega} & V^{K} \bar{K}^{*} \rightarrow \eta \omega & V^{\eta \phi \rightarrow \eta \omega}=0 \\
V^{\pi \rho \rightarrow K \bar{K}^{*}} & V^{\eta \omega \rightarrow K \bar{K}^{*}} & V^{K \bar{K}^{*} \rightarrow K \bar{K}^{*}} & V^{\eta \phi \rightarrow K \bar{K}^{*}} \\
V^{\eta \phi \rightarrow \pi \rho}=0 & V^{\eta \omega \rightarrow \eta \phi}=0 & V^{K \bar{K}^{*} \rightarrow \eta \phi} & V^{\eta \phi \rightarrow \eta \phi}
\end{array}\right)
$$

## Diagrams and Parameters

Channels involved : $\pi \rho, \eta \omega, K \bar{K}^{*}$ and $\eta \phi$.

|  | meson | channel | IS | $\lambda(\mathrm{MeV})$ | $n$ |
| :--- | :---: | :---: | ---: | ---: | :---: |
| $\pi \rho \rightarrow \pi \rho$ | $\pi$ | $u$ | -8 | 600 | 1 |
| $\pi$ | $\rho$ | $t$ | -8 | 600 | 1 |
| $\pi \rho \rightarrow K \bar{K}^{*}\left(\bar{K} K^{*}\right)$ | $\omega$ | $u$ | 4 | 600 | 2 |
| $K$ | $u$ | $\sqrt{6}(-\sqrt{6})$ | 1500 | 1 |  |
| $K \bar{K}^{*} \rightarrow K \bar{K}^{*}$ | $K^{*}$ | $t$ | $\sqrt{6}(-\sqrt{6})$ | 1110 | 1 |
|  | $\rho$ | $t$ | -3 | 1050 | 1 |
| $K \bar{K}^{*} \rightarrow \bar{K} K^{*}$ | $\omega$ | $t$ | -1 | 1050 | 1 |
|  | $\phi$ | $t$ | -2 | 1700 | 1 |
|  | $\pi$ | $u$ | 3 | 1050 | 1 |
|  | $\eta$ | $u$ | 3 | 1050 | 1 |
|  | $\rho$ | $u$ | -3 | 1050 | 2 |
|  | $\omega$ | $u$ | -1 | 1050 | 2 |
|  | $\phi$ | $u$ | -2 | 1700 | 2 |

*All same as in $a_{1}$ channel except IS values

## Diagrams and Parameters

Channels involved : $\pi \rho, \eta \omega, K \bar{K}^{*}$ and $\eta \phi$.

|  | meson | channel | IS | $\lambda(\mathrm{MeV})$ | $n$ |
| :--- | :---: | :---: | ---: | ---: | ---: |
| $\pi \rho \rightarrow \eta \omega$ | $\rho$ | $u$ | -4 | 600 | 2 |
| $\eta \omega \rightarrow \eta \omega$ | $\omega$ | $u$ | $4 / 3$ | 600 | 2 |
| $\eta \omega \rightarrow K \bar{K}^{*}\left(\bar{K} K^{*}\right)$ | $K$ | $u$ | $-\sqrt{6}(\sqrt{6})$ | 940 | 1 |
|  | $K^{*}$ | $t$ | $-\sqrt{6}(\sqrt{6})$ | 940 | 1 |
| $K \bar{K}^{*}\left(\bar{K} K^{*}\right) \rightarrow \eta \phi$ | $K$ | $u$ | $2 \sqrt{3}(-2 \sqrt{3})$ | 940 | 1 |
|  | $K^{*}$ | $t$ | $2 \sqrt{3}(-2 \sqrt{3})$ | 940 | 1 |
| $\eta \phi \rightarrow \eta \phi$ | $\phi$ | $u$ | $16 / 3$ | 1400 | 2 |

*Note that for $\phi$-exchange diagram the coupling $g_{2}$ differ by about $11 \%$

## $h_{1}$ resonance



We compare the model to experimental data from charge exchange reaction $\pi p \rightarrow 3 \pi n$.


And define:

$$
\sigma \equiv-C \operatorname{Im}\left[T_{\pi \rho}\left(M_{\pi \rho}\right)\right]
$$

Exp.Data : J.A.Dankowych, PRL46 (1981). Model: G.Janssen, PRC54 (1996)

## $h_{1}$ properties

- The $h_{1}(1170)$ pole position, $\sqrt{s_{R}}=1152.3-i 162.7[\mathrm{MeV}]$
- Residue and coupling strength can be defined as

$$
\lim _{s \rightarrow s_{R}}\left(s-s_{R}\right) T_{a, b}=R_{a, b}, \quad g_{a}=\sqrt{R_{a, a}}
$$

- The elastic residue of $h_{1}(1170)$ resonance for $S$-wave and $D$-wave are

|  | $S$-wave | $D$-wave | Unit |
| :--- | :---: | :---: | :---: |
| $R_{\pi \rho}$ | $17.84-i 10.75$ | $0.31+i 0.01$ | $\mathrm{GeV}^{2}$ |
| $R_{\eta \omega}$ | $16.57+i 6.40$ | $0.08+i 0.04$ | $\mathrm{GeV}^{2}$ |
| $R_{K \bar{K}^{*}}$ | $24.86+i 2.26$ | $-0.02+i 0.22$ | $\mathrm{GeV}^{2}$ |
| $R_{\eta \phi}$ | $70.88-i 12.89$ | $0.96+i 0.10$ | $\mathrm{GeV}^{2}$ |

## $G=+1$ and $I=1$

## $b_{1}$ resonance

## Diagrams and Parameters

Channels involved : $\pi \omega, \pi \phi, \eta \rho$ and $K \bar{K}^{*}$.

$$
\left|K \bar{K}^{*}(+)\right\rangle=\frac{1}{\sqrt{2}}\left(\left|K \bar{K}^{*}\right\rangle+\left|\bar{K} K^{*}\right\rangle\right)
$$

Potential :

$$
V^{f i}=\left(\begin{array}{cccc}
V^{\pi \omega \rightarrow \pi \omega} & V^{\pi \phi \rightarrow \pi \omega}=0 & V^{\eta \rho \rightarrow \pi \omega} & V^{K \bar{K}^{*} \rightarrow \pi \omega} \\
V^{\pi \omega \rightarrow \pi \phi}=0 & V^{\pi \phi \rightarrow \pi \phi}=0 & V^{\eta \rho \rightarrow \pi \phi}=0 & V^{K \bar{K}^{*} \rightarrow \pi \phi} \\
V^{\pi \omega \rightarrow \eta \rho} & V^{\pi \phi \rightarrow \eta \rho}=0 & V^{\eta \rho \rightarrow \eta \rho} & V^{K} \bar{K}^{*} \rightarrow \eta \rho \\
V^{\pi \omega \rightarrow K \bar{K}^{*}} & V^{\pi \phi \rightarrow K} \bar{K}^{*} & V^{\eta \rho \rightarrow K \bar{K}^{*}} & V^{K} \bar{K}^{*} \rightarrow K \bar{K}^{*}
\end{array}\right)
$$

## Diagrams and Parameters

Channels involved : $\pi \omega, \pi \phi, \eta \rho$ and $K \bar{K}^{*}$.

|  | meson | channel | IS | $\lambda(\mathrm{MeV})$ | $n$ |
| :---: | :---: | :---: | ---: | ---: | :---: |
| $K \bar{K}^{*} \rightarrow K \bar{K}^{*}$ | $\rho$ | $t$ | 1 | 1050 | 1 |
|  | $\omega$ | $t$ | -1 | 1050 | 1 |
| $K \bar{K}^{*} \rightarrow \bar{K} K^{*}$ | $\phi$ | $t$ | -2 | 1700 | 1 |
|  | $\pi$ | $u$ | 1 | 1050 | 1 |
|  | $\eta$ | $u$ | -3 | 1050 | 1 |
|  | $\rho$ | $u$ | -1 | 1050 | 2 |
|  | $\omega$ | $u$ | 1 | 1050 | 2 |
|  | $\phi$ | $u$ | 2 | 1700 | 2 |

*All same as in $a_{1}$ channel

## Diagrams and Parameters

Channels involved : $\pi \omega, \pi \phi, \eta \rho$ and $K \bar{K}^{*}$.

|  | meson | channel | IS | $\lambda(\mathrm{MeV})$ | $n$ |
| :--- | :---: | :---: | ---: | ---: | :---: |
| $\pi \omega \rightarrow \pi \omega$ | $\rho$ | $u$ | 4 | 600 | 2 |
| $\pi \omega \rightarrow \eta \rho$ | $\omega$ | $u$ | $4 / \sqrt{3}$ | 600 | 2 |
| $\pi \omega \rightarrow K \bar{K}^{*}\left(\bar{K} K^{*}\right)$ | $K$ | $u$ | $\sqrt{2}(\sqrt{2})$ | 660 | 1 |
|  | $K^{*}$ | $t$ | $\sqrt{2}(\sqrt{2})$ | 660 | 1 |
| $\pi \phi \rightarrow K \bar{K}^{*}\left(\bar{K} K^{*}\right)$ | $K$ | $u$ | $-2(-2)$ | 610 | 1 |
|  | $K^{*}$ | $t$ | $-2(-2)$ | 610 | 1 |
| $\eta \rho \rightarrow \eta \rho$ | $\rho$ | $u$ | $4 / 3$ | 600 | 2 |
| $\eta \rho \rightarrow K \bar{K}^{*}\left(\bar{K} K^{*}\right)$ | $K$ | $u$ | $\sqrt{6}(\sqrt{6})$ | 560 | 1 |
|  | $K^{*}$ | $t$ | $\sqrt{6}(\sqrt{6})$ | 560 | 1 |

## $b_{1}$ resonance



We compare the model to experimental data from charge exchange reaction $\pi p \rightarrow \omega \pi n$.

And define:

$$
\sigma \equiv-C \operatorname{Im}\left[T_{\pi \omega}\left(M_{\pi \omega}\right)\right]
$$

Exp.Data: S.Fukui, PLB257 (1991)

## $b_{1}$ properties

- The $b_{1}(1235)$ pole position, $\sqrt{s_{R}}=1307.6-i 61.9[\mathrm{MeV}]$
- Residue and coupling strength can be defined as

$$
\lim _{s \rightarrow s_{R}}\left(s-s_{R}\right) T_{a, b}=R_{a, b}, \quad g_{a}=\sqrt{R_{a, a}}
$$

- The elastic residue of $b_{1}(1235)$ resonance for $S$-wave and $D$-wave are

|  | $S$-wave | $D$-wave | Unit |
| :--- | :---: | :---: | :---: |
| $R_{\pi \omega}$ | $4.72+i 4.82$ | $0.02+i 0.03$ | $\mathrm{GeV}^{2}$ |
| $R_{\pi \phi}$ | $10.36+i 8.33$ | $0.00+i 0.00$ | $\mathrm{GeV}^{2}$ |
| $R_{\eta \rho}$ | $8.13+i 7.94$ | $0.00+i 0.00$ | $\mathrm{GeV}^{2}$ |
| $R_{K \bar{K}^{*}}$ | $117.80-i 60.23$ | $-0.03+i 0.09$ | $\mathrm{GeV}^{2}$ |

## Summary and Conclusion

- We investigated the axial-vector meson resonance from pseudoscalar and vector meson interaction based on the fully off-mass-shell coupled channel formalism.
- By doing so, we generate $a_{1}, h_{1}$ and $b_{1}$ axial-vector meson dynamically.
- We also present the comparison of the model calculation to the experimental data from charge exchange reaction and we extracted the resonance properties of $a_{1}, h_{1}$ and $b_{1}$ axial-vector meson.
- For the future project, we will investigate $S= \pm 1$ channel.


## Thank You

